

The Econometrics of Social Interactions and Networks

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Norms in Agricultural Tenancy Contracts, Burke and Young (2001)

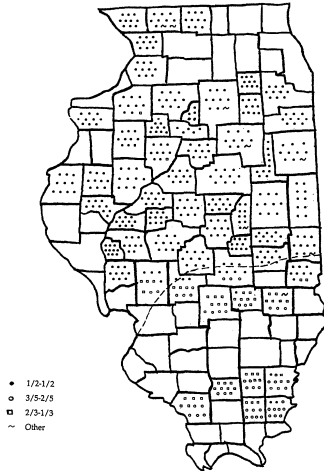


FIGURE 4. DISTRIBUTION OF SHARE CONTRACTS BY COUNTY: ILLINOIS, 1995

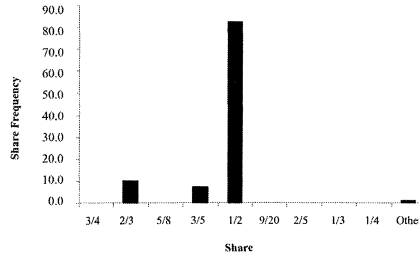


FIGURE 1. CROP SHARE FREQUENCIES IN ILLINOIS:
TENANT'S SHARE OF THE CORN CROP
(Frequencies in percent)

Source: Illinois Cooperative Agricultural Extension Service *Farm Leasing Survey*, 1995.

Neighborhood Racial Composition Changes, Card, et al. (2008)

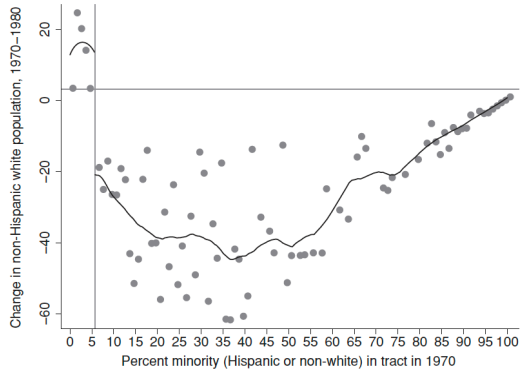
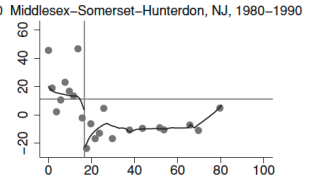
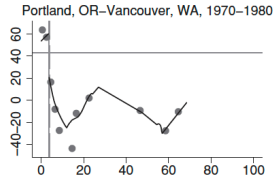
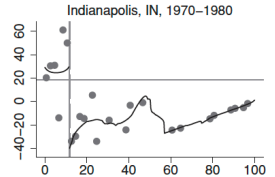
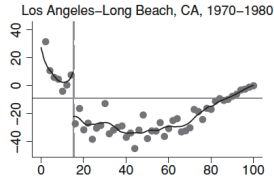


FIGURE I
Neighborhood Change in Chicago, 1970-1980

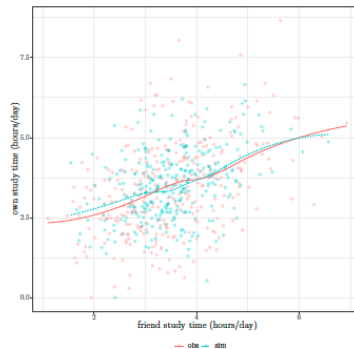


Study Time Among College Students, Conley et al. (2023)

Table 2: Study time and GPA OLS regressions

	<i>Dependent variable:</i>	
	Own study	GPA
	(1)	(2)
Male	-0.369** (0.171)	-0.131* (0.076)
Black	0.116 (0.214)	-0.225** (0.109)
HS GPA	0.413** (0.188)	0.437*** (0.081)
ACT	-0.032 (0.023)	0.040*** (0.013)
HS study	0.043*** (0.008)	0.001 (0.004)
Expected study	-0.002 (0.009)	-0.006 (0.003)
Friend study	0.166*** (0.039)	
Own study		0.090*** (0.022)
Constant	1.915** (0.759)	0.417 (0.362)
Observations	574	571
R ²	0.169	0.259

Figure A4: Fit of own study time against friend study time



Social Interactions

- ▶ Commonality: others' choices matter for individual's outcomes and/or choices, and are *not* mediated by markets/prices.
- ▶ Economists refer to these as settings involving **social interactions**.
 - ▶ Old question in the social sciences: the interrelationship between the group and the individual.
- ▶ Wide array of phenomena: crime, teen behavior, school performance, addictions, learning, fads, public good provision, social norms, residential choice, etc.
 - ▶ Cross-group vs. within-group variance differences.
 - ▶ Individual-level variation in characteristics unable to account for variation across the population.
 - ▶ Unifying approach: social networks.

Social Interactions: Main Ingredients

1. A social network: \mathbf{A} , a_{ij} indicates i and j influence each other (study partners).
 - ▶ In some settings, \mathbf{A} is known and fixed: (doesn't mean exogenous!: sorting).
 - ▶ In other settings, interest is in how \mathbf{A} arises: network formation.
2. Some outcome of interest y_i (academic achievement).
3. Some treatment or choice of interest ω_i (study time).
 - ▶ Others' choices ω_j matter for own choice ω_i : 'endogenous (peer) effects'.
4. Observed individual characteristics x_i (sex).
 - ▶ Others' characteristics x_j matter for own choice ω_i : 'contextual effects'.
5. Unobserved individual characteristics ϵ_i (conscientiousness).
 - ▶ Others' characteristics ϵ_j dependent with own characteristics ϵ_i : 'correlated effects'.

Micro-founded Workhorse Linear Model, Blume et al. (2015)

- ▶ Linear-quadratic utility:

$$U = \left(\gamma x_i + \epsilon_i + \delta x_{A(i)} \right) \omega_i - \frac{\phi}{2} \left(\omega_i - \omega_{A(i)} \right)^2 - \frac{1}{2} \omega_i^2$$

defining

$$x_{A(i)} \equiv \sum_{j: a_{ij} > 0} a_{ij} x_j \quad \omega_{A(i)} \equiv \sum_{j: a_{ij} > 0} a_{ij} \omega_j.$$

- ▶ δ : strength of contextual effects.
- ▶ ϕ : strength of peer effects. In this case, preference for conformity.
- ▶ γ : standard 'own' effect.
- ▶ ϵ_i unobserved by us and i 's social network \Rightarrow game of incomplete info.

Linear Best Reply, Blume et al. (2015)

- Leads to a linear ‘best reply’:

$$\omega_i = \frac{\gamma}{1+\phi} x_i + \frac{\delta}{1+\phi} x_{A(i)} + \frac{\phi}{1+\phi} \mathbb{E}[\omega_{A(i)} | x_i, \epsilon_i] + \frac{1}{1+\phi} \epsilon_i$$

and solving for the social equilibrium,

$$\boldsymbol{\omega}^* = \frac{1}{1+\phi} \left(I - \frac{\phi}{1+\phi} \mathbf{A} \right)^{-1} [\gamma I + \delta \mathbf{A}] \mathbf{x} + \boldsymbol{\nu}$$

which has the ‘reduced-form’ form

$$\omega_i = \pi_1 x_i + \pi_2 x_{A(i)} + \nu_i$$

Identification I: Reduced Form

$$\omega_i = \pi_1 x_i + \pi_2 x_{A(i)} + \nu_i \quad (1)$$

- ▶ π_2 captures both direct and social network (indirect) influences on i 's choice:
 - ▶ Sex of study partners $x_{A(i)}$ directly affects i 's marginal utility of studying.
 - ▶ Sex of study partners $x_{A(i)}$ directly affects their marginal utility of studying, and thus indirectly i 's pressure to conform to his peers' study hours.
- ▶ From (1) we cannot separately identify (δ, γ, ϕ) .
 - ▶ $\phi \neq 0$: social feedback effects: Manski (1993) called it the 'reflection problem'.
 - ▶ But if $\text{cov}(x_{A(i)}, \nu_i) = 0$ and we can reject $H0 : \pi_2 = 0$, we have evidence of some kind of social interaction (contextual or peer).

Identification II: Correlated Unobservables

- ▶ $cov(x_{A(i)}, \nu_i) = 0$: very strong assumption.
- ▶ ν_i is a linear combination of the unobservables of i and i 's social network.
- ▶ Own observables likely dependent with own unobservables: students with higher high school GPA possibly more conscientious.
- ▶ Friend's unobservables likely dependent with own unobservables: i sorts into a study group of conscientious students.

Social Interactions III: Correlated Unobservables

- ▶ When the problem generating $\text{cov}(x_{A(i)}, \nu_i) \neq 0$ is sorting of similar people into groups, a possibility is to do an intervention that **randomizes group composition**.
- ▶ This breaks the dependence between others' unobservables and individual characteristics.
- ▶ See e.g., [Sacerdote \(2001\)](#): random assignment of roommates in a college.
- ▶ But beware of re-sorting post intervention!: see [Carrell, Sacerdote, West \(2013\)](#): Air Force Academy experiment.

Social Interactions IV: Correlated Unobservables

- ▶ When the problem generating $\text{cov}(x_{A(i)}, \nu_i) \neq 0$ is the presence of common environmental factors (crime, quality of schools, quality of governance, etc), the problem is perhaps more serious.
 - ▶ E.g., Men likely to study with men, and men study near the soccer field, which is noisy and distracting.
 - ▶ Perhaps the reason for the recent work estimating 'neighborhood effects' (e.g. Chetty and coauthors).
 - ▶ Or quasi-natural experiments (instruments) that generate variation in $x_{A(i)}$:
 - ▶ Note: can look for variation in the x_j' 's (see e.g., [Acemoglu, Garcia-Jimeno, Robinson \(2015\)](#)), or in the $A(i)$ (see e.g., [Garcia-Jimeno, Iglesias, Yildirim \(2022\)](#)).

Social Multipliers I: Glaeser et al (1996), (2003)

- ▶ Alternative way to look for evidence of social interactions: social multipliers.
 - ▶ In the presence of social interactions (even just contextual effects), individual level causal relationship \neq aggregate level 'equilibrium' relationship.
 - ▶ E.g., If one additional hour of study time causes a 0.1 pp increase in GPA, the slope of a group-level regression of average study time on average GPA will have a slope much higher than 0.1.
 - ▶ For simplicity, suppose $\phi = 0$, $x_i \perp \epsilon_i$, and that people interact in disjoint groups g .
 - ▶ Individual-level reduced-form regression: $\omega_{ig} = a + bx_{ig} + \eta_{ig}$.
 - ▶ Group-level regression (average within groups): $\bar{\omega}_g = \tilde{a} + \tilde{b}\bar{x}_g + \bar{\eta}_g$
 - ▶ Glaeser et al. define the social multiplier as: $S = \frac{\tilde{b}}{b}$.

Social Multipliers II

- ▶ Since the social interactions model is

$$\omega_{ig} = \gamma x_{ig} + \delta \bar{x}_g + \epsilon_{ig} \Rightarrow \text{plim}(b) = \gamma + \delta \frac{\text{cov}(x_{ig}, \bar{x}_g)}{\text{var}(x_{ig})}$$

- ▶ Averaging the social interactions model,

$$\bar{\omega}_g = (\gamma + \delta) \bar{x}_g + \bar{\epsilon}_g \Rightarrow \text{plim}(\tilde{b}) = \gamma + \delta$$

Social Multipliers III

- \Rightarrow Social multiplier:

$$S = \frac{\gamma + \delta}{\gamma + \delta \frac{\text{cov}(x_{ig}, \bar{x}_g)}{\text{var}(x_{ig})}}$$

- If segregation across groups is perfect, then $\text{cov}(x_{ig}, \bar{x}_g) = \text{var}(x_{ig})$, and
- In the other extreme, if membership to $S=1$ groups is randomly assigned, then $\text{cov}(x_{ig}, \bar{x}_g) = 0$, and

$$S = \frac{\gamma + \delta}{\gamma}$$

- The more similar people are within a group, the lower the multiplier.

Social Multipliers IV: Dartmouth Randomly Assigned Roommates

TABLE 1. SOCIAL MULTIPLIERS IN FRATERNITY PARTICIPATION
 DARTMOUTH ROOMMATE DATA: EFFECT OF BACKGROUND CHARACTERISTICS ON PARTICIPATION
 IN FRATERNITIES AT THE INDIVIDUAL LEVEL AND THREE LEVELS OF AGGREGATION

	(1) Member of fraternity or sorority	(2) Room average level membership	(3) Floor average membership	(4) Dorm average membership
Drank beer in high school	0.1040 (0.0258)	0.0984 (0.0399)	0.1454 (0.0812)	0.2320 (0.1930)
Constant	0.0482 (0.1455)	0.1980 (0.2266)	0.7993 (0.4594)	2.2277 (1.1421)
R-squared	0.04	0.05	0.03	0.08
Observations	1579	700	197	57
Average group size	1	2.3	8.0	28

Notes: Data are for Dartmouth Freshmen. Roommates and dormmates are randomly assigned as described in Sacerdote (2001). Regressions include math and verbal SAT scores, dummy for male, family income, high school GPA. SAT scores are from Dartmouth Admissions data. Family income, use of beer, and high school GPA are self reported on the UCLA Higher Education Research Institute’s Survey of Incoming Freshmen. Standard errors in parentheses. Column (1) shows the OLS regression of individual fraternity participation on own use of beer in high school. (Own SAT scores, own high school GPA and own family income are also included but not shown). Column (2) regresses the average participation at the dorm room level on dorm room averages of high school beer use, SAT scores, HS GPAs, and family income. Columns (3) and (4) increase the level of aggregation to the dorm floor and dorm building, respectively.

Experimental Approaches: Randomization

- ▶ Settings where researchers may conjecture that social interactions are present (e.g. spillovers of a program):
 - ▶ Distinction between **direct** and **indirect** treatment effects -analogous to own and contextual effects- (see [Manski \(2013\)](#) for a general framework).
- ▶ Ideally, randomization should break the dependence of own treatment x_i with unobservables, but also of social network's treatments $x_{A(i)}$ with unobservables.
 - ▶ Issue 1: How to do this?
 - ▶ Issue 2: Non-compliance: Even if you randomly assign a treatment, people may not take it up (for reasons related to their unobservables).

Social Interactions Moral Hazard: Kremer and Miguel (2007)

- ▶ An insightful example is the work by Kremer and Miguel (2007) who use data from an intervention in Kenyan schools to incentivize de-worming of children (see also Beaman et al. (2021)).
- ▶ Experimental design:
 - ▶ 3 sets of schools, staggered randomized treatment \Rightarrow schools comparable.
 - ▶ Treatment: de-worming drugs and lots of training.
 - ▶ Ask parents how many other parents they know with children in the different schools.
- ▶ Idea: compare child de-worming drug take-up decisions of parents (T_i) in later-treated schools that have different numbers of social connections to parents of children in the early treatment schools.
 - ▶ How many other parents you know is endogenous, but how many of those are in early schools is exogenous thanks to randomization.

Social Interactions Moral Hazard: Kremer and Miguel (2007)

$$\mathbb{P}(T_i = 1) = \delta x_{A(i)} + \beta_1 N_i + \beta_2 Z_i + \epsilon_i$$

- ▶ $x_{A(i)}$: How many parents with children in treated schools I know.
- ▶ N_i : How many other parents I know.
- ▶ Notice that the children in early-treated schools are **not** in this regression sample.

What if we try estimating a peer effect with nonexperimental data?

NONEXPERIMENTAL SOCIAL EFFECT ESTIMATES (GROUPS 2 AND 3)

	Dependent variable: Child took deworming drugs in 2001		
	(1)	(2)	(3)
Explanatory variables:			
Proportion deworming drug take-up in 2001, respondent's own school (not including respondent)	0.852*** (0.107)		
# parent links with children in respondent's own school whose children received deworming		0.016 (0.011)	
# parent links with children in early treatment schools whose children received deworming and had "good effects"			0.004 (0.025)
# parent links with children in early treatment schools whose children received deworming and had "side effects"			-0.152* (0.080)
# parent links with children in early treatment schools whose children received deworming and respondent does not know effects			0.003 (0.049)
# parent links with children in early treatment schools whose children did not receive deworming			-0.006 (0.055)
# parent links with children in early treatment schools, respondent does not know whether they received deworming			-0.010
Total social link controls, socio-economic controls	Yes	Yes	Yes
Number of observations (parents)	1,678	886	886
Mean of dependent variable	0.61	0.56	0.56

Social Interactions Moral Hazard: Kremer and Miguel (2007) results

EXPERIMENTAL SOCIAL EFFECT ESTIMATES

	Dependent variable: Child took deworming drugs in 2001				
	(1)	(2)	(3)	(4)	(5)
Explanatory variables:					
# parent links with children in early treatment schools (Groups 1 and 2, not own school)	-0.031** (0.014)	-0.040** (0.017)			-0.002 (0.018)
# parent links with children in early treatment schools		0.017 (0.029)			
* Group 2 school indicator					
Proportion direct (first-order) parent links with children in early treatment schools			-0.098** (0.045)		
# parent links with children in early treatment schools, with whom respondent speaks at least twice/week				-0.030** (0.016)	
# parent links with children in early treatment schools, with whom respondent speaks less than twice/week				-0.033 (0.033)	
# parent links with children in Group 1, 2, or 3 schools, not own school, with whom respondent speaks at least twice/week				0.008 (0.012)	
# parent links with children in Group 1, 2, or 3 schools, not own school, with whom respondent speaks less than twice/week				0.026 (0.027)	
# parent links with children in early treatment schools					-0.0062* (0.0032)
* Respondent years of education					
# parent links with children in Group 1, 2, or 3 schools, not own school	0.013 (0.011)	0.012 (0.017)	-0.006 (0.009)		-0.014 (0.014)
# parent links with children not in Group 1, 2, or 3 schools	-0.007 (0.007)	-0.008 (0.009)	-0.005 (0.007)	-0.007 (0.007)	-0.008 (0.011)
# parent links, total	0.019*** (0.005)	0.029*** (0.007)	0.021*** (0.007)	0.018*** (0.005)	0.013 (0.008)

Example: Displacement Effects of Labor Market Policies

- ▶ Crepon et al. (2013) study a large-scale job-seeker assistance program in France.
- ▶ In DiTraglia et al. (2023) we revisit it.
- ▶ They randomized offers of intensive job placement services.
- ▶ The issue:
 - ▶ *Job seekers who benefit from counseling may be more likely to get a job, but at the expense of other unemployed workers with whom they compete in the labor market. This may be particularly true in the short run, during which vacancies do not adjust: the unemployed who do not benefit from the program could be partially crowded out.*

How can we test whether such displacement effects are present?:

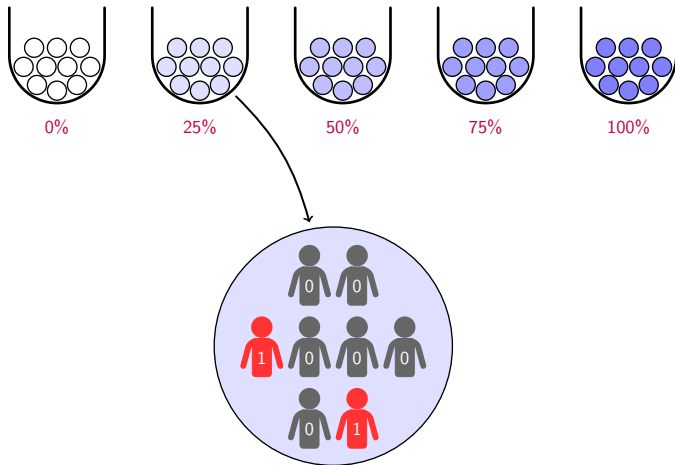
Randomized Saturation Designs

Partial Interference

Spillovers within but not between groups.

Randomized Saturation

Two-stage experimental design.



Randomized Saturation Experiments

Sample Size and Indexing

Groups $g = 1, \dots, G$

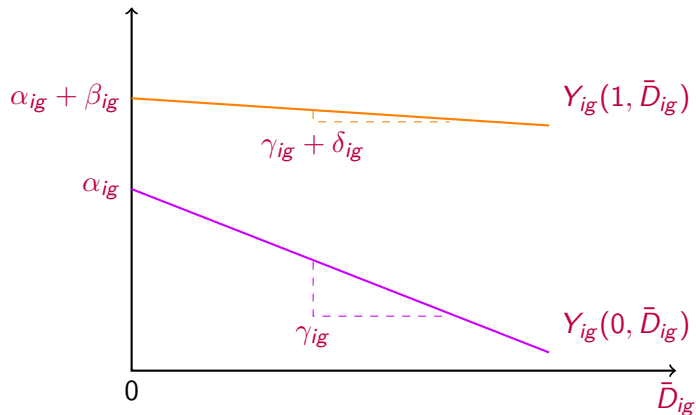
Individuals in g $i = 1, \dots, N_g$

Observables

Y_{ig}	outcome of (i, g)
$Z_{ig} \in \{0, 1\}$	treatment offer to (i, g)
$D_{ig} \in \{0, 1\}$	treatment take-up of (i, g)
$\bar{D}_{ig} \in [0, 1]$	take-up of (i, g) 's “neighbors”
$S_g \in \mathcal{S} \subseteq [0, 1]$	saturation of group g

Linear Model allowing for heterogeneous effects:

$$Y_{ig}(D_{ig}, \bar{D}_{ig}) = \alpha_{ig} + \beta_{ig}D_{ig} + \gamma_{ig}\bar{D}_{ig} + \delta_{ig}D_{ig}\bar{D}_{ig}$$



Indirect Effects

Treated: $\gamma_{ig} + \delta_{ig}$

Untreated: γ_{ig}

Direct Effects

$\beta_{ig} + \delta_{ig}\bar{D}_{ig}$

Randomized Saturation Experiments

- ▶ Intuitively, each layer of randomization provides exogenous variation for each effect (own and spillover).
- ▶ However: Need to be careful:
 1. IOR: Need to rule out **spillovers in take-up**:

$$D_{ig}(Z_i, Z_{-i}) = D_{ig}(Z_i).$$

2. The “naive IV” will not work: need to condition on the share of compliers \overline{C}_g in one's group.
 - ▶ Under RSD, share of neighbors offered treatment is exogenous.
 - ▶ Under IOR, share of neighbors taking up is $\overline{D}_g \approx \overline{C}_g \times S_g$.

Testing the IOR assumption in the Crepon et al. (2013) experiment

(IOR) + (1-Sided)

Take-up only depends on *own* offer:

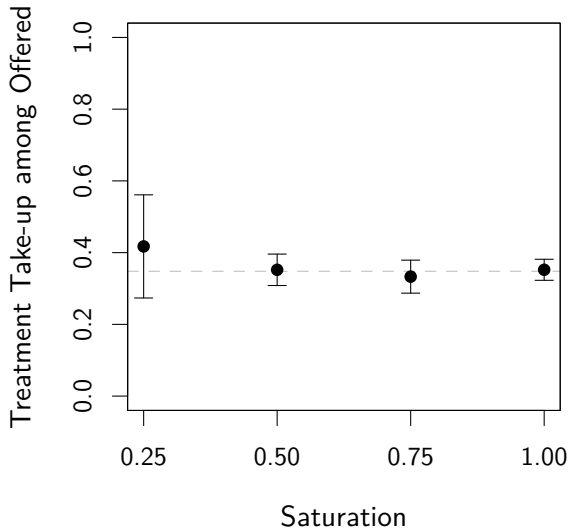
$$D_{ig} = C_{ig} \times Z_{ig}$$

Testable Implication

$$\mathbb{E}[D_{ig}|Z_{ig} = 1, S_g] = \mathbb{E}[D_{ig}|Z_{ig} = 1]$$

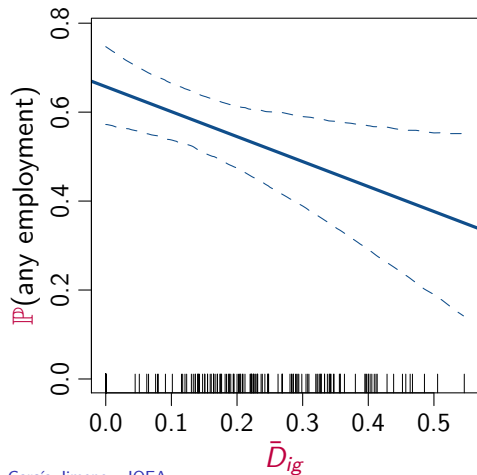
Figure at right

Take-up among offered doesn't vary with saturation ($p = 0.62$)

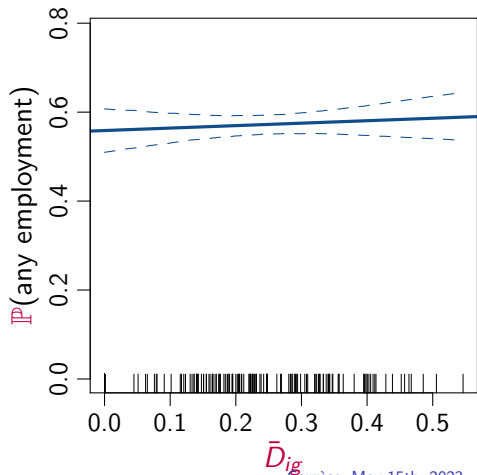


Displacement and Shielding Effects in the Crepon et al. (2013) experiment

Untreated: $\mathbb{E}[Y_{ig}(0, \bar{d}) | \text{Complier}]$



Treated: $\mathbb{E}[Y_{ig}(1, \bar{d}) | \text{Complier}]$



Non-experimental Approaches: Instrumental Variables

- ▶ Two examples using quasi-experimental variation to identify social interaction effects.
 1. Exogenous cross-sectional variation in the contextual variable x_i , hence in $x_{A(i)}$ (see Bramoulle, Djebbari, Fortin (2009)). State capacity and public good provision.
 2. Exogenous time series variation in network connections $A(i)$ (hence in $x_{A(i)}$): Information diffusion and collective action.

State Capacity: Acemoglu, Garcia-Jimeno, Robinson (2015)

- ▶ Social interactions may be present in the provision of public goods and the development of state infrastructure too.
- ▶ In [Acemoglu, Garcia-Jimeno, Robinson \(2015\)](#) how investments in public infrastructure in a municipality may matter for investments in nearby municipalities in Colombia.
- ▶ Both model the investment choices, and use colonial state presence measures as instruments.
- ▶ Municipality chooses investment ω_i to maximize 'prosperity':

$$p_i = (\gamma_1 x_i + \epsilon_i) \omega_i + \phi \omega_i \omega_{A(i)} + \gamma_2 \omega_{A(i)} + u_i - \frac{\theta}{2} \omega_i^2$$

- ▶ Allow for direct spillover effects of public goods from neighboring municipalities.

Best Responses and Equilibrium

- ▶ Investment choice (best response):

$$\omega_i = \frac{\phi}{\theta} \omega_{A(i)} + \gamma_1 x_i + \epsilon_i \quad (2)$$

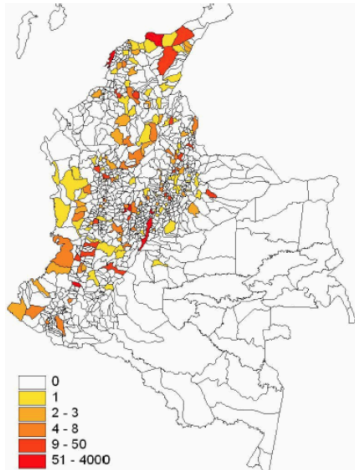
- ▶ So the *equilibrium* relationship between prosperity and investments is

$$p_i = \theta \omega_i^2 + \gamma_2 \omega_{A(i)} + u_i \quad (3)$$

- ▶ Estimate **both** (2) and (3) using IVs:
 - ▶ An element of x_i is colonial state presence.
 - ▶ If $x_i \Rightarrow \omega_i$, then $x_{A(i)} \Rightarrow \omega_{A(i)}$.
 - ▶ Exclusion restriction: $\text{cov}(x_{A(i)}, \epsilon_i) = 0$.

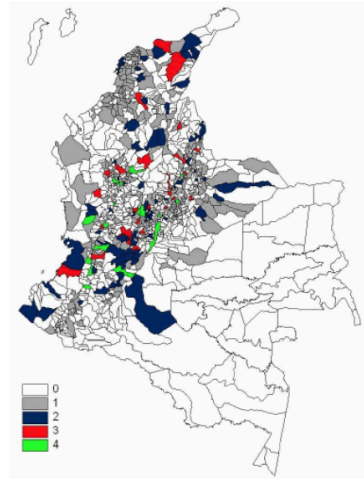
The Spanish Colonial State in 18th Century Colombia

Crown Employees



Source: Duran y Díaz (1794)

State Agencies



Source: Duran y Díaz (1794)

Acemoglu, Garcia-Jimeno, Robinson (2015): Estimates

TABLE 3—CONTEMPORARY STATE EQUILIBRIUM BEST RESPONSE

State capacity measured as log of:	Equilibrium best response							
	Number of state agencies				Number of municipality employees			
	OLS (1)	IV (2)	IV (3)	Sys. GMM (4)	OLS (5)	IV (6)	IV (7)	Sys. GMM (8)
<i>Panel I</i>								
ds_i/ds_j	0.016 (0.002)	0.017 (0.003)	0.019 (0.003)	0.020 (0.003)	0.021 (0.003)	0.022 (0.004)	0.022 (0.004)	0.016 (0.003)
$ds_i/d(\text{colonial state officials}_i)$	0.127 (0.031)	0.128 (0.031)	0.108 (0.033)	−0.040 (0.050)	0.129 (0.043)	0.130 (0.043)	0.105 (0.047)	0.087 (0.069)
$ds_i/d(\text{colonial state agencies}_i)$	0.003 (0.033)	0.001 (0.033)	−0.016 (0.033)	0.096 (0.055)	0.017 (0.058)	0.017 (0.059)	−0.002 (0.060)	0.085 (0.085)
$ds_i/d(\text{distance to royal roads}_i)$	0.008 (0.019)	0.010 (0.019)	0.007 (0.021)	0.074 (0.034)	−0.035 (0.034)	−0.035 (0.035)	−0.038 (0.036)	−0.036 (0.044)

TABLE 4A—PROSPERITY AND PUBLIC GOODS STRUCTURAL EQUATION

<i>Panel I</i>	State capacity measured as: log of number of municipality state agencies							
	Prosperity equation							
	Life quality index				Public utilities coverage			
	OLS (1)	IV (2)	IV (3)	Sys. GMM (4)	OLS (5)	IV (6)	IV (7)	Sys. GMM (8)
dp_i/ds_i	0.802 (0.044)	0.394 (0.135)	0.389 (0.143)	0.314 (0.041)	0.602 (0.037)	0.563 (0.127)	0.567 (0.134)	0.314 (0.041)
dp_i/ds_j	0.015 (0.004)	0.024 (0.006)	0.025 (0.006)	0.025 (0.004)	0.022 (0.004)	0.020 (0.006)	0.020 (0.006)	0.027 (0.003)

Collective Action and Information: Garcia-Jimeno, et al. (2022)

- ▶ Social networks play important role in information diffusion.
- ▶ Collective action (e.g., protest movements) requires lots of coordination, which in turn requires information transmission.
- ▶ We study the spread of the Temperance Crusade, an anti-liquor protest movement in the 1870s.

Collective Action and Information: Garcia-Jimeno, et al. (2022)

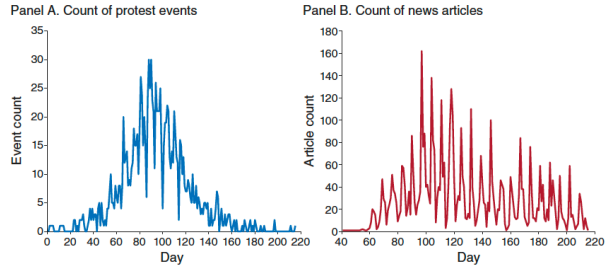


FIGURE 1. TEMPERANCE CRUSADE ACTIVITY AND ITS NEWSPAPER COVERAGE, DECEMBER 1873–JULY 1874

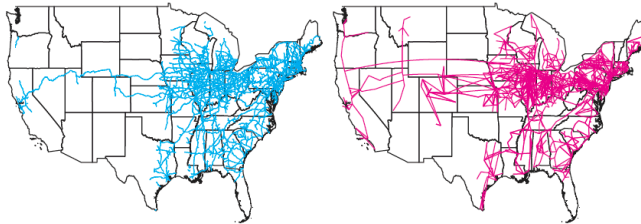


FIGURE 2. THE RAILROAD AND TELEGRAPH NETWORKS, c.1870

Collective Action and Information: Garcia-Jimeno, et al. (2022)

- Model the protest events as pieces of information, and the railroad and telegraph networks as the links over which the information is transmitted:

$$\omega_{it} = \beta_r^\ell \omega_{R_t(i), t-\ell} + \beta_\gamma^\ell \omega_{\Gamma_t(i), t-\ell} + \epsilon_{it}$$

- Use railroad accidents that disrupt the communications network to construct **time-varying** instruments for rail and telegraph connected towns.

Railroad Accidents and Variation in Connectivity

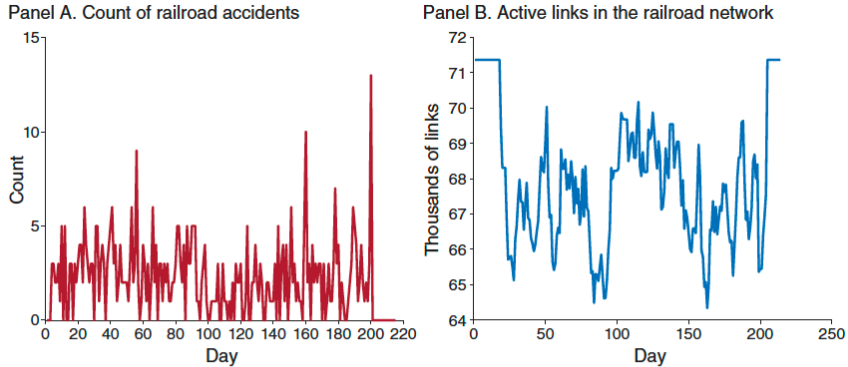


FIGURE 3. VARIATION IN RAILROAD ACCIDENTS: NUMBER OF ACCIDENTS AND ACTIVE LINKS IN THE RAILROAD NETWORK, DECEMBER 1873–JULY 1874

Garcia-Jimeno, et al. (2022): Results

TABLE 2—THE EFFECT OF INFORMATION ALONG THE RAIL AND TELEGRAPH NETWORKS: CAUSAL ESTIMATES

	Any crusade activity a_{it} —meetings, petitions, marches					
	5 days			3 days		
	OLS (1)	IV (2)	GMM (3)	OLS (4)	IV (5)	GMM (6)
First lag rail ($\mathbf{r}_{i,t} \mathbf{a}_{t-1}$)	0.004 (0.001)	0.037 (0.013)	0.038 (0.013)	0.005 (0.001)	0.032 (0.014)	0.031 (0.016)
First lag telegraph ($\gamma_i \mathbf{a}_{t-1}$)	0.014 (0.006)	0.172 (0.033)	0.163 (0.054)	0.008 (0.005)	0.072 (0.015)	0.076 (0.039)
Second lag telegraph ($\gamma_i \mathbf{a}_{t-2}$)	0.018 (0.005)	−0.068 (0.031)	−0.053 (0.058)	0.011 (0.004)	0.020 (0.024)	0.014 (0.034)
Third lag distance ($\mathbf{d}_i \mathbf{a}_{t-3}$)	0.001 (0.0001)	0.006 (0.002)	0.006 (0.002)	0.001 (0.0001)	−0.001 (0.001)	−0.001 (0.001)
Number of towns	15,934	15,934	15,934	15,950	15,950	15,950
Maximum number of periods	16	16	16	30	30	30
Observations	267,247	267,247	267,247	487,548	487,548	487,548

Network Formation

- ▶ Economists are also interested in understanding where **A** comes from: how are social connections produced? E.g., high-school friendships, trading relations, co-authoring relationships, etc.
- ▶ A starting point is a conditionally independent dyadic model:

$$a_{ij} = f(x_i, x_j, u_i, u_j, v_{ij})$$

- ▶ a_{ij} = link (friendship), x_i = observed characteristics of i (PSG vs. Marseille fan), u_i = unobserved characteristics of i (sociability), v_{ij} a pair-specific unobserved shock (same church –easier–, or having a friend in common –harder–).
- ▶ In general, $x_i \not\perp u_i$.

Network Formation: Issues

- ▶ $a_{12} \perp a_{34}$: Friendship decisions of disjoint pairs are independent: knowing that 1 and 2 are friends provides no information about whether 3 and 4 are friends.
 - ▶ $a_{12} \not\perp a_{13}$: both influenced by x_1, u_1 : E.g., 1 is a grumpy person. Observing that 1 is not friends with 2 suggests 1 is unlikely to be friends with 3.
 - ▶ $a_{12} \not\perp a_{13} | x_1$: both link decisions still influenced by u_1 .
 - ▶ $a_{12} \not\perp a_{21}$:
 - ▶ Links do not need to be symmetric (e.g., I cite you, you don't cite me).
 - ▶ $a_{12} \not\perp a_{21} | x_i, x_j, u_i, u_j$: If v_{ij}, v_{ji} covary, still dependence.
- ⇒ Running a dyadic OLS/Probit regression (e.g., Santos Silva and Tenreiro (2010)) will be a problem:
1. Bias: Covariates x_i, x_j 's dependent with the error u_i, u_j, v_{ij} .
 2. Inference: errors across dyad observations $(i, j), (i, k)$ dependent.

Network Formation: Example of Bias

- ▶ Model of friendships with **homophily**: teenagers more likely to be-friend other teenagers of the same race (x_i) (see [Miyauchi \(2016\)](#)).
- ▶ Also, some teenagers more sociable than others (u_i).

$$a_{ij} = \mathbf{1} \{ \phi \mathbf{1} \{ x_i = x_j \} + u_i + u_j + v_{ij} > 0 \}$$

- ▶ Three students, same race, all friends with each other: $a_{12} = a_{13} = a_{23} = 1$.
- ▶ Suppose we ignore u_i, u_j : \Rightarrow attribute all three links to a preference for homophily (large ϕ), although maybe 1 and 3 became friends not because they are both the same race but because A is very sociable (large u_i).

Solutions: Graham (2017)

- ▶ u_i, u_j are **nuisance parameters**: In a relatively sparse network, each u_i only matters for a relatively small number of links \Rightarrow cannot just use individual fixed effects.
- ▶ When v_{ij} are logit errors,

$$\ell_{ij} = \mathbb{P}(a_{ij} = 1 | \phi, u_i, u_j) = \frac{\exp(\phi x_{ij} + u_i + u_j)}{1 + \exp(\phi x_{ij} + u_i + u_j)}$$

- ▶ Graham (2017) offers two possible solutions.

Solutions: Graham (2017)

- ▶ 1. Conditional likelihood: Find a sufficient statistic such that conditioning on it, the likelihood of the network does *not* depend on the u_i anymore.
 - ▶ The **degree sequence** $S = (d_1, d_2, \dots, d_N)$ of the network happens to be such a sufficient statistic.

$$L = \mathbb{P}(\mathbf{A}|\phi, S) = \prod_{ij} \ell_{ij} = \frac{\exp(\sum_{ij} a_{ij} \phi x_{ij})}{\sum_{\alpha \in D} \exp(\sum_{ij} \alpha_{ij} \phi x_{ij})},$$

$$D_S = \{\text{Adjacency matrices } \mathbf{A} \text{ with degree sequence } S\}.$$

Solutions: Graham (2017)

- ▶ 2. Fixed point problem:

- ▶ First fix a ϕ and find the solution to

$$\mathbf{U}(\phi) = \operatorname{argmax} \mathbb{P}(\mathbf{A}|\phi, u_1, \dots, u_N).$$

- ▶ Then find the solution to

$$\phi^* = \operatorname{argmax} \mathbb{P}(\mathbf{A}|\phi, \mathbf{U}(\phi))$$

- ▶ Iterate.

- ▶ See [Islam et al. \(2022\)](#) for an application to a Bangladeshi friendship network.

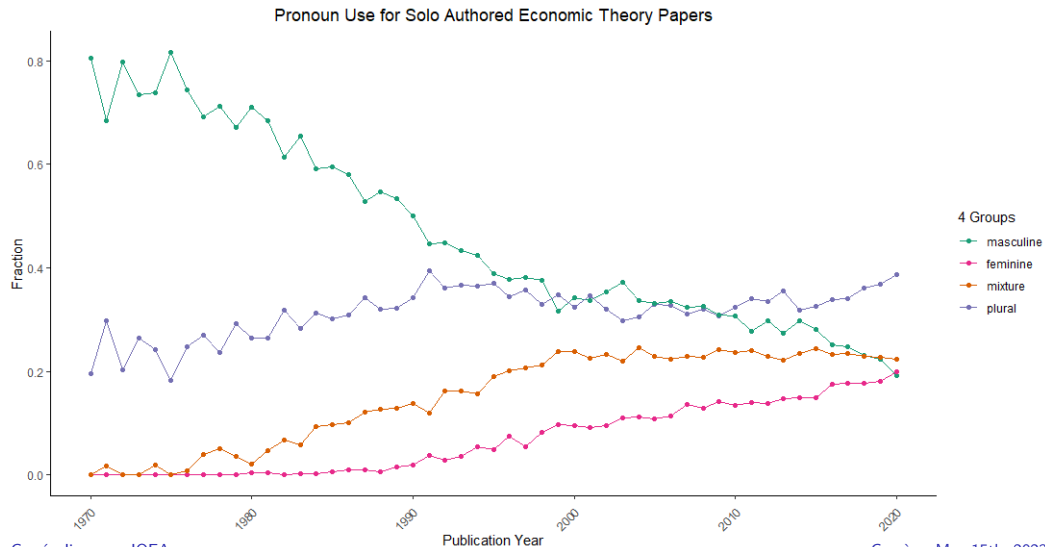
Community Detection

- ▶ Community Detection: Methods to classify nodes in a network that are the same type –belong to the same community– (see [Karrer and Newman \(2010\)](#)).
- ▶ In our notation, find which nodes have the same u_i , when u_i indexes groups.
- ▶ Methods based on statistical inference develop efficient algorithms to find the best possible partition of nodes into a fixed number of groups to maximize

$$\mathbb{P}(\mathbf{A}|\phi, u_1, \dots, u_N)$$

- ▶ E.g., Social norms (I'm working on): Co-authorship network of economists.
 - ▶ 2 groups: liberals and conservatives.
 - ▶ Homophily in co-authorship decisions.
 - ▶ Use the recovered classification to control for u_i in a social interactions model of pronoun gender choice.

Pronoun Gender Choice



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